MAT135H1F – REVIEW CHECKLIST

1. Limits

1.1. Basics.

- (1) definition of limits at $a \in \mathbb{R}$, at $\pm \infty$,
- (2) vertical and horizontal asymptotes (what are these and how do you find them),
- (3) limit laws, substitution property, simple tricks to calculate limits,
- (4) squeeze theorem (what is it and how do you apply it).

1.2. L'Hospital's rule.

- (1) statement,
- (2) types of indeterminate forms (quotients, differences, products and powers),
- (3) how to deal with these indeterminate forms (i.e. transoforming powers to products by taking ln).

1.3. Important limits.

(1) rational functions, a^x when a < 1 or a > 1 and $x \to \pm \infty$,

(2)
$$\frac{e^x}{\text{polynomial}}, \frac{\ln(x)}{\text{polynomial}},$$

(3) $\frac{\sin(x)}{x}$ and $\frac{1-\cos(x)}{x}.$

1.4. Continuity.

- (1) definition,
- (2) types of discontinuities, examples and their graphs,
- (3) sums, products and compositions of continuous functions are continuous,
- (4) IVT and how to apply it to find roots of continuous functions.

2. DIFFERENTIATION

2.1. Basics.

- (1) definition of the derivative,
- (2) meaning of the derivative as the slope of tangent, velocity, marginal cost and instantaneous rate of change,
- (3) equation of tangent lines,
- (4) differentiable implies continuous but not the other way. Example!

You have to know the derivatives of elementary functions and their inverses back and forth!

2.2. Rules of differentiation.

- (1) product rule,
- (2) quotient rule,
- (3) chainrule (!).

2.3. Implicit differentiation.

- (1) how to find tangent lines to curves given by implicit formulas,
- (2) finding the derivative of inverses,
- (3) differentiating complicated formula using logartihmic differentiation,
- (4) derivatives of $f(x)^{\overline{g}(x)}$ type functions (logarithmic differentiation).

2.4. Rolle's theorem and MVT.

- (1) statement of Rolle's theorem and the MVT,
- (2) consequences about functions with 0 derivative and functions with equal derivative,
- (3) how do you apply Rolle's theorem to show that a function only has at most 1, 2, 3... roots?

3. Applications

3.1. Finding local max and mins.

- (1) what are critical points,
- (2) definition of local and global extreme values,
- (3) definition of concave up and down, inflection points,
- (4) EVT and Fermat's theorem,
- (5) closed interval method,
- (6) 1st derivative test for local max and min,
- (7) 2nd derivative test for local max and min.

3.2. Exponential growth and decay.

- (1) exponential growth model and the relative rate of growth,
- (2) radioactive decay model and half-life,
- (3) what is the number e?
- (4) continuously compounded interest.

3.3. Optimization.

- (1) how to find global maxima and minima?
- (2) first derivative test for global max and mins,

3.4. Related Rates.

- (1) How to connect the known and unknown quantities?
- (2) Implicit differentiation for the rates of change.

3.5. Sketching curves.

- (1) definition of increasing and decreasing,
- (2) checklist for sketching curves (!),
- (3) increasing, decreasing test (sign of the 1st derivative),
- (4) testing concavity and finding inflection points (sign of 2nd derivative),
- (5) how to find vertical, horizontal and slant asymptotes.

 $\mathbf{2}$

3.6. Antiderivatives.

- (1) what is an antiderivative? (definition),
- (2) antiderivatives of the simplest functions (see textbook).